Star Chinese School, Rhode Island 罗得岛星星中文学校



<u> 数学教学大纲 Math Syllabus (2017-2018 学年度)</u>

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# THE GOLDEN RULE: "ALWAYS TRY YOUR BEST"

# **Class Requirements:**

- Student should come to class with the following materials:
- o Textbook o Notebook
- o PENCIL
- Completed Assignments
- o 1 Pocket Folder o Graphing Calculator (only for Algebra II, III, and precalculus)

Class Hours: 11:30 am to 12:30 pm on Saturdays, Sept. 09, 2017-June 16, 2018

# **Expectations:**

- ➤ We expect you to arrive to class on time.
- > We expect you to take notes and keep a notebook or binder.
- > We expect you to try your best on all assignments and tests.
- > We expect you to participate CONSTRUCTIVELY in class.
- > We expect you to follow instructions.
- > NO TALKING is allowed unless given permission.
- > NO FOOD, DRINKS, and GUM are allowed in the classroom.

> NO CELL PHONES, I-PODS, or other electronic devices are allowed in the classroom without teacher's permission.

\*All school rules are in effect at all times.\*

## **Grading Policy:**

Your grade in Math course will be determined by your performance on tests (40%), quizzes (25%), homework (20%), and exams (15%).

## Make Up Policy

It is the students' responsibility to locate the teacher, determine what has been missed, and complete any make- up work.

# **Arithmetic I**

## Textbook: ARITHMETIC THE EASY WAY

## **Course Description**

This is a yearlong course with a goal to improve students' skills in arithmetic at the beginners' level of mathematics. In this course, we will review and explain the basic ideas and skills of basic mathematics, such as counting numbers, addition, subtraction, multiplication, and division. We will have many examples to understand the concepts and to practice the skills. We would like to improve the students' confidence to handle more advanced mathematics problems.

#### **Major Topics**

#### Number

- Numbers as symbols
- Counting
- o Even and Odd numbers
- o Old Systems of Numbering

#### Addition

- o The Language of Addition
- o The Number Line
- o Unequal Addition
- o Place value
- Know the Combinations

- The language of Subtraction
- o Unequal Subtractions
- o Exchanging in Subtraction

#### Multiplication

- o Multiplying Whole Numbers;
- Combinations
- Multiplication Applied to Measuring

#### Division

- o The Language of Division
- o Zero as a Place Holder
- o Carrying Remainders
- *Dividing by More than a One-digit Number*

#### Subtraction

# **Arithmetic II**

Text book: "Barron's Arithmetic - The easy way", 4th Edition

**Scope:** Arithmetic II is a class for third grade to fifth grade students who have learned the basic math concepts including four major math operations, namely addition, subtraction, multiplication and division. It covers the textbook contents from Chapter 6 to Chapter 15 involving fractions, decimals, percents and measurements as well as their applications. **Major Topics** 

#### First Class/New Student Enrollment

- Get to Know Each Other
- School and Class Policies
  - Test to See What You Know about Math

#### Arithmetic I Review

- Test Review
- Recommendations to Students/Parents for Class Adjustment Upon Individual Student Knowledge Level

#### Chapter 6 The Important Parts – Fractions

- S6.1 What is a Fraction?
- S6.2 The Language of a Fraction
- S6.3 What Kinds of Fractions Are There?

Chapter 6 The Important Parts – Fractions

- S6.4 Simplifying Fractions
- S6.5 Equivalent Fractions
- S6.6 Which Fraction is Larger or Smaller?

#### Chapter 6 The Important Parts – Fractions

- S6.7 Changing Improper Fractions to Mixed Numbers
- S6.8 Changing Mixed Numbers to Improper Fractions
- Chapter Test 6

#### Chapter 7 Piece by Piece – Adding Fractions

- S7.1 Fractions Can be Added
- S7.2 After Adding, What Next?
- S7.3 Fractions Whose Sum is One

• S7.4 Fractions Whose Sum is Greater Than One

#### Chapter 7 Piece by Piece – Adding Fractions

- S.7.5 Mixed Numbers Can Also Be Added
- S7.6 Mixed Numbers Whose Sum May Be Simplified
- S7.7 Mixed Numbers Whose Fractional Parts Add Up to One
- S7.8 Mixed Numbers with Fractional Parts Whose Sum is Greater Than One Chapter 7 Piece by Piece – Adding Fractions
- S7.9 Word Problems
- S7.10 What About Those Denominators?
- S7.11 Mixing Them All Up
- S7.12 More Difficult Word Problems

#### Chapter 7 Piece by Piece – Adding Fractions

- Chapter 7 Quiz
   Chapter 8 Subtracting
   Fractions
- S8.1 Subtracting Fractions
- S8.2 After Subtracting, What Next?
- S8.3 Like Fractions Whose Difference is One or Greater Than One
- S8.4 Mixed Numbers Can Also Be Subtracted
- S8.5 Exchanging in Subtracting Fractions

#### Chapter 8 Subtracting Fractions

- S8.6 Exchanging in Subtracting Mixed Numbers (Like Denominators)
- S8.7 Word Problems

- S8.8 Subtracting Fractions with Unlike Denominators
- S8.9 Subtracting Mixed Numbers
- S8.10 Exchanging in Subtracting Mixed Numbers (Unlike Denominators)

# Chapter 8 Subtracting Fractions

- S8.11 More Difficult Word Problems
- Chapter Test 8

#### Chapter 9 Multiplying and Dividing Fractions

- S9.1 The Product of Two Fractions
- S9.2 Cancellation
- S9.3 Finding Parts of Whole Numbers
- S9.4 Multiplying Three or More Fractions

# Chapter 9 Multiplying and Dividing Fractions

- S9.5 Multiplying Mixed Numbers
- S9.6 Word Problems
- Chapter 9 Multiplying and
- Dividing Fractions
  - S9.7 The Quotient of Two Fractions
  - S9.8 Dividing Mixed Numbers

# Chapter 9 Multiplying and Dividing Fractions

- S9.9 Word Problems
- Chapter Test 9

## Chapter 10 What's the Point? Decimals

- S10.1 Introducing Decimals
- S10.2 Reading and Writing Decimals

#### Chapter 10 What's the Point? Decimals

- S10.3 Which Fraction Equals Which Decimal?
- S10.4 Comparing Decimals

Chapter 10 What's the Point? Decimals

- S10.5 Rounding Off Decimals
- Chapter Test 10

# Chapter 11 Adding and

#### Subtracting Decimals

- S11.1 Adding Decimals
- S11.2 Adding Mixed Decimals
- S11.3 Word Problems Requiring the Addition of Decimals
- S11.4 Subtracting Decimals
- S11.5 Subtracting Mixed Decimals
- S11.6 Word Problems Requiring the Subtraction of Decimals

#### Chapter 12 Multiplying Decimals

- S12.1 Multiplying a Decimal by a Whole Number
- S12.2 Multiplying Decimal Numbers
- S12.3 Special Multipliers of 10, 100, 1000, and so on
- S12.4 Word Problems Requiring the Multiplication of Decimals

# Chapter 12 Multiplying Decimals

• Chapter Test 12

#### Chapter 13 Dividing Decimals

- S13.1 Dividing a Decimal by a Whole Number
- S13.2 Zero as a Place Holder in the Quotient

## Chapter 13 Dividing Decimals

- S13.3 Changing a Fraction into a Decimal
- S13.4 Dividing a Decimal by a Decimal
- S13.5 Zero as a Place Holder in the Dividend

Chapter 13 Dividing Decimals

- S13.6 Word Problems Requiring the Division of Decimals
- S13.7 Special Divisors of 10, 100, 1000, and so on

#### **Chapter 13 Dividing Decimals**

- S13.8 Changing a Decimal into a Fraction
- S13.9 Rewriting Decimals with Fractions

#### Chapter 13 Dividing Decimals

- S13.10 Word Problems Combining Fractions and Decimals
- Chapter Test 13

## Chapter 14 Percents

- S14.1 Meaning of Percent
- S14.2 Changing Percents to Decimals

# Chapter 14 Percents

- S14.3 Changing Decimals to Percents
- S14.4 Changing Percents to Fractions
- S14.5 Changing Fractions to Percents

## Chapter 14 Percents

- S14.6 Finding a Percent of a Number
- S14.7 Finding the Percent That One Number is of Another Chapter 14 Percents
- S14.8 Finding a Number When a Percent of It Is Known
- Chapter Test 14 Chapter 15 Measurement
  - S15.1 Units of Measurement
  - S15.2 Adding Measures
  - S15.3 Subtracting Measures
  - S15.4 Multiplying Measures
  - S15.5 Dividing Measures

- S15.6 Word Problems Requiring Measures
- S15.7 Converting Metric Measures Math Competition

Semester Review Final Exam

# Algebra Part I

#### **Course Description**

This course is for students who are currently in grade 5 to 6 at regular school. The goal of this course is to improve students' skills in pre-Algebra and part of algebra I, which is difficult time for all the beginners to learn Algebra. In this course, first we will review Arithmetic II, such as fraction, decimal, percent, and some examples in the real life. Then we'll learn pre-algebra and part of algebra I.

#### **Reference book**:

- 1. Barron's E-Z PRE-ALGEBRA. New
- 2. Barron's E-Z ALGEBRA. New
- 3. "Barron's Math The easy way", 4th Edition. Old book, as reference.

## Major Topics

# Pre-algebra part:

#### I. Numbers and Order of Operations

- o Numbers and Sets
- o Properties of numbers
- o Order of operations

#### **II. Fractions**

- Equivalent Fractions
- o Common Factors (GCF and LCM)
- o Operation of Rational Numbers
- Operation of Mixed Numbers
- Word Problems

#### **III. Decimals**

- Rounding off Decimals
- Terminating and Repeating Decimals
- Operation of Decimals
- o Word Problems

## **IV. Integers**

- o Definition of Integers
- Operation of Negative Numbers

#### **V. Ratios and Proportions**

- o Definition of Ratio?
- o Writing and Solving Ratios
- What is a Rate?
- Rates (Unit Rate, Unit price, Best price)
- What is a Proportion?
- o Solving proportions
- o Word Problems

#### **VI.** Percents and Percentages

- o Definition of Percent
- o Calculate a Percent
- Word Problems (Percent Increase or Decrease)

Grade and Math Fun and Parents Meeting Graduation Ceremony/Annual Picnic

#### VII. Converting of Fractions, Decimals,

#### VIIII. Roots and Real Numbers

- The Square Roots
- o Irrational Numbers
- o Fractional Exponents

# Algebra I part:

#### I. The Language and Tools of Algebra

- Variables and Expressions
- Order of Operations
- o Identity and Equality
- Properties
- o The Distributive, Commutative
- and Associative Property
- o Basic Expressions and

#### Equations

- o Verbal Expressions into
- algebraic Expressions
- Substitution Property of Equality

# Algebra Part II

Reference: Barron's E-Z ALGEBRA. Plus the instructor copied material.

#### **Major Topics**

- 1. Exponents
- O Exponents and Scientific Notation
- o Law of Exponents
- 2. Roots and Real Number
- Square root and Pythagorean Theorem

#### **II. Solving Linear Equations**

- o Write Equations
- o Solving Equations by Using
- Addition and Subtraction
- Solving Equations by Using
- Multiplication and Division
- o Solving MultiStep Equations
- o Solving Equations with
- variables on Both sides
- o Ratio and Proportions
- o Percent of Change
- o Solving for a Specific Variable
- o Solving Absolute Value

Equations

o Word Problems

#### **III. Algebra-More on Equations**

- o Inequalities
- **o** Graphs of Equations
- Slope of a Line
- o Fraction square root
- *Square root properties*
- 0 Higher index roots
- 3. Algebraic Expressions
- O Monomials, Binomials, and Trinomials
- o Simplifying Algebraic Expressions
- o Multiplying Binomials
- 4. Functions
- o Function Notation
- o Calculating a Function
- 5. Graphs
- o Domain and Range of a Function

- Independent and Dependent Variables
- o Points and Distance
- o Linear Equation Graphing
- The Slope of a Line
- o Graphing Inequalities
- o Graphing Relationships
- 6. System of Equations
- o Solving one Variable Equation

# Algebra Part III

Reference: Barron's E-Z ALGEBRA

#### **MajorTopics**

#### **Solving Linear Inequalities Systems**

- Solving Systems of Equations
- o Solving Systems of Inequalities
- by Graphing
- o Linear Programming
- Solving Systems of Equation in Tree Variables

#### Matrices

- o Operations with Matrices
- o Multiplying Matrices
- o Transformations with Matrices
- 0 Determinants
- o Cramer' Rule
- o Identity and Inverse Matrices
- o Using Matrices to Solve System
- of Equations

#### **Polynomials**

- o Roots of Real Number
- o Radical Expression
- o Rational Exponents
- o Radical Equations and

Inequalities

o Complex Number

#### **Quadratic Functions and Inequalities**

- Graphing Quadratic Functions
  Solving Quadratic Equations by Graphing
- Solving Quadratic Equations by Factoring
- Complete the Square

- Two Equation System
- Solving Two Equation System
- 7. Quadratic Equations
- Solving by Inspection
- Solving by Quadratic Formula
- Solving by Completing the Square

- The Quadratic Formula and
- Discriminant
- Analyzing Graphs of Quadratic
- Function
- Graphing and Solving
- Quadratic Inequalities

#### **Polynomials Functions**

- Graphing Polynomials
- Functions
- Solving Equations Using
- Quadratic Techniques
- o The Remainder and Factor
- Theorems
- o Roots and Zeros
- o Rational Zero Theorem
- o Operations on Functions
- o Inverse Functions and
- Relations
- Square Root Functions and
- Inequalities

#### Trigonometric

- o Right Triangle Trigonometry
- o Angles and Angle Measurement
- o Trigonometric Function of
- General Angle (Unit Circle)

#### **Statistics and Probability**

- Sampling and Bias
- Counting Outcomes
- o Permutations and
- *Combinations*

Probability of Compound Events
Probability Distributions

# **PreCalculus**

## Textbook: Pre-Calculus The Easy Way

## Reference:

- 1. Fred Safier, Schaum's Outlines: Theory and Problems of Precalculus (2<sup>nd</sup> edition), McGrawHill, 2009
- 2. Ron Larson & Robert Hostetler, Precalculus, Houghton Mifflin Company, 2007

# Topics and time schedule:

# **Chapter 1 Preliminaries (Oct)**

- Standard form of polynomials
- Factoring polynomials
- Operations on exponents
- o Rational expressions
- Radical expressions

# Chapter 2 Graph of Linear &

# **Quadratic Equations** (Oct. –Nov.)

- Coordinate systems
- *Slope, intercept, midpoint & distance formula*
- o Graph of linear equation
- Graph of linear equations

• Complex numbers & quadratic formula

o Graph of quadratic equations

# **Chapter 3 Functions and Graphs**

(Dec.-Jan.)

- o Functions and Their Properties
- o Twelve Basic Functions
- Building Functions from Functions
- Graphical Transformations
- Modeling and Equation Solving

#### **Chapter 4 Exponential and Logarithmic** (Feb.-Mar.)

# **Chapter 6 Conic Sections** (May-June)

- Midpoint and Distance Formula
- o Parabolas
- o Circles
- 0 Ellipses

- o Exponential Functions
- Logarithms and Logarithmic
- o Properties of Logarithms
- Common Logarithms
- Base e and Natural Logarithms Functions

# **Chapter 5 Rational Expressions and Equations** (Mar.-Apr.)

- Operations of Rational
- Expressions
- o Graphing Rational Functions
- Direct, Joint and Inverse
- Variation
- Solving Rational Equations and Inequalities

# Chapter 5 Sequences and Series (May)

- Arithmetic Sequence & Series
- o Geometric Sequence & Series
- Basic Combinatory
- Probability
- o The Binomial Theorem
- Recursion and Special
- Proof and Mathematical Induction
- Hyperbolas
- Conic Sections
- o Solving Quadratic

# Geometry

# Course Goals:

This course is for students who is currently taking or is going to take their first course in Geometry at regular school. It deals with questions of size, shape, and relative position of figures. This is an introduction of important concepts and principles in Geometry. The goal is to develop a logical structure in which mathematical relationships are proved as well as applied.

# Course Objectives:

- 1. Appreciate fundamental concepts and principles in Geometry
- 2. Solve problems using these principles
- 3. Identify a wide range of topics related to Geometry
- 4. Address specific Geometry problems

# Teaching Methods and Assignments corresponding to Objectives:

- 1. Generously using drawings and examples in descriptions of Geometry concepts
- 2. Including all steps in proving theorems to help students understanding the way to

prove a mathematical relationship

- 3. Presenting a wide range of example problems
- 5. Group discussions on some relative complex problems
- 6. Assignments for each week
- 7. A total of four tests

# Text book:

"E-Z Geometry" by Lawrence S. Leff

## Lectures Schedule:

	Class	Title			
Fundamental Definitions and Postulates					
	1	Fundamental definitions and postulates			
	No Class				

Measure and Congruence				
	2	Measuring segments and angles		
	3	Properties of equality and congruence		
Angle Pairs and Perpendicular Lines				
	4	Angle pairs and theorems relating to angle pairs		
	5	Perpendicular lines and right angles		
Parallel lines				
	6	Properties of parallel lines		
	7	Parallel postulates		
	8	Review		
	9	Test I		
Angles of Polygon				
	10	Theorems relating to angles of triangles		
	Thanksgiving Holiday			
	11	Theorems relating to angles of polygons		
Proving Triangles are Congruent				
	12	Proving triangles congruent		
	13	Proving overlapping triangles congruent		
	Christmas holiday			
	New year holiday			
Applying Congruent Triangles				
	14	Using congruent triangle to prove segments and angles congruent		
	15	Using congruent triangle to prove special properties of lines		
	16	Isosceles triangle and double congruence proofs		
	17	Review		
	18	Test II		

Special Quadrilaterals					
	19	Properties of parallelogram			
	20	Proving parallelogram			
	21	Application of parallelogram			
Ratio, Proportion, and Similarity					
	22	Ration and proportion			
	23	Proving triangles similar			
	24	Proportions in similar triangles			
	25	Proportions in right triangles			
	26	Proportions in right triangles-continue			
	27	Review			
	28	Test III			
Circles and Angle Measurement					
	29	Properties of circles			
	30	Angle measurement theorems			
	31	Continue angle measurement theorems			
Chord, Tangent, and Secant Segment					
	32	Concepts of chords, tangent, and secant			
	33	Chord and tangent relationship			
Area and Volume					
	No class, Math Competition				
	34	Areas of polygon			
	35	Areas of circle and sector			
	36	Review			
	37	Test IV			
	38	Review			